# The relation of raindrop size to intensity of rainfall in different types of tropical rain using a simple raindrop recorder

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ABSTRACT. The paper gives the results of studies of raindrop size characteristics in three other different types of tropical rain to what Sivaramakrishnan had earlier studied (1961), using the simple raindrop recorder. The study of raindropsize characteristics refers to analysis of raindrop samples taken at Poona in (1) typical shower types of rain without thunder (cumuliform clouds), (2) continuous type of rain with occasional thunder (cumuliform and stratiform clouds mixed) and (3) non-freezing rain during typical monsoon from stratiform clouds. Regression equations connecting the intensity of rainfall with the various rainfall parameters such as median drop size  $D_n$ , liquid water content W, radar reflectivity Z have been developed and compared with findings of other investigators all over the world. Best's formula is found to represent the size distribution of raindrops in the tropics also but with suitable changes in the constants. It is also shown in agreement with results obtained earlier by Sivaramakrishnan (1961), Blanchard (1953), Best (1951), Atlas and Chmela (1957) and Spilhaus (1948) that the median drop diameter is the most suitable parameters such as mean diameter  $D_m$ , mode diameter  $D_d$ , mean volume diameter  $D_d$  and predominant diameter  $D_p$ .

#### 1. Introduction

Considerable study has been made during the last few years of raindrop spectra and their relation to the average size of raindrop, liquid water content W and radar reflectivity Z. Basic references on the subject are the papers of Laws and Parsons (1943), Marshall and Palmer (1948), Spilhaus (1948), Best (1950, 1951), Blanchard (1953), Jones (1956), Mueller and Jones (1960), Fujiwara (1960), Atlas (1963). Sivaramakrishnan has given an up-to-date survey of raindrop distribution (1961) including data for tropical storms, showers and continuous type of rain.

The effects of evaporation, coalescence, wind sorting on drop size distribution have been considered by Rigby, Marshall and Hitschfeld (1954), Gunn and Marshall (1955), Imai *et al.* (1955), Imai (1956), Atlas and Chmela (1957), Sivaraman and Sivaramakrishnan (1962). The available evidence from all the above papers clearly shows that drop size spectra are highly variable in time, space and with type of rainfall.

The present study refers to the analysis of raindrop size characteristics of rain samples taken at Poona during (a) typical shower type of rain without thunder (from cumuliform clouds), (b) continuous type of rain with occasional thunder (from stratiform and cumuliform clouds mixed) and (c) non-freezing rain during typical monsoon rain from stratiform clouds.

Regression equations connecting the intensity of rainfall with the various rainfall parameters such as average size of raindrop, liquid water content W, radar reflectivity Z, have been developed and compared (Table 4) with the findings of other investigators - Boucher (1951), Higgs (1952), Kelkar (1961), Srivastava (1960). It is shown in agreement with the results obtained earlier by Spilhaus (1948), Best (1951), Blanchard (1953), Atlas and Chmela (1957), and Sivaramakrishnan (1961) that the median drop diameter is the most suitable parameter for describing the average size of the drop size distribution in preference to other average size parameters such as mean diameter  $D_m$ , mode diameter  $D_d$ , mean volume diameter  $D_v$  and the predominant diameter  $D_p$ .

Best's formula for the size distribution of raindrop given by --

$$1 - F = \exp\left[-(x/a)^n\right]$$
 (1)

where  $a = A/R'^p$ 

F = Fraction of liquid water in the air comprised by drops with diameter less than x

#### $\mathbf{B}' = \text{Rate of rainfall}$

#### A, p and n are constants

is found to be suitable for representing the size distribution of raindrops in the tropics also but with suitable changes in Best's constants.

#### 2. Verification of Best's formula

From Best's equation, it can be shown that log  $\log_{10} [1/(1-F)] = -0.36 + n (\log_{10}x - \log_{10}a) (2)$ 

If Eq. (1) represents the data and  $\log \log_{10} [1/(1-F)]$ is plotted against  $\log_{10} x$  the points should lie on a straight line with slope n. From the intercept of this line on the  $\log \log_{10} [1/(1-F)]$  axis, the value of  $(0.36 + n \log_{10} a)$  and hence of a can be obtained. Figs. 1 and 2 give sections of raindrop records with corresponding self-recording Siphon raingauge record during a heavy shower on 17 September 1960 without thunder and continuous type of rain with occasional thunder on 19 September 1960 (from stratiform and cumuliform clouds mixed). In the bottom of Figs. 1 and 2, log log10 [1/(1-F)] on Y axis and on the X axis the corresponding dropsize  $\log x$  has been plotted. The points when joined is found to be a straight line showing that Best's formula for the drop size distribution is found to be suitable for the drop size distribution in tropical rains also.

#### 3. Results

A complete description of the raindrop recorder has been given in Sivaramakrishnan's earlier paper (1961), giving the method of obtaining a continuous record of the time of occurrence, duration of different types of rain and range of raindrop sizes using a dyed filter paper tape technique. Tables 1, 2, 3 and 5 give a summary of the following raindrop parameters taken with the raindrop recorder during (a) shower type of rain from cumuliform clouds, (b) continuous type of rain with thunder from stratiform and cumuliform clouds mixed and (c) continuous non-freezing rain from stratiform clouds at Poona, where—

1. 
$$R' = \text{Rate of rainfall (mm/hr)}$$
  
= 6  $\pi$  10<sup>-4</sup>  $\Sigma$  N<sub>D</sub> D<sup>3</sup>  $\delta$ DV, where

V = Terminal velocity of drop size D(m/sec),  $N_D =$  number of drops between diameter limits per unit volume of air (per cubic metre) and

D = drop diameter (mm)

- 2.  $W = \text{Liquid water content} \pmod{(\text{mgm/m}^3)}$ =  $\frac{1}{6} \pi \Sigma N_D D^3 \delta D$
- 3.  $Z = \text{Radar reflectivity factor } (\text{mm}^6/\text{m}^3)$ =  $\Sigma N_D D^6 \delta D$
- 4.  $D_n$  = Median volume diameter (*i.e.*, value of that drop diameter which divides the drop distribution into two parts such that each represents half of the liquid water content W)
- 5. D = Predominant diameter (the diameter corresponding to the maximum volume of water per unit interval of diameter range, *i. e.*, the diameter for which  $\delta F/\delta x$  of 'Best' formula is greatest)

- 6.  $D_m =$  Mean diameter (*i.e.*, the sum of all drop diameters divided by the number of drops)
- D<sub>d</sub> = Mode diameter (*i.e.*, the diameter corresponding to the maximum number of drops)
- 8.  $D_v$  = Mean volume diameter, *i.e.*, diameter of a drop whole volume is equal to the average drop volume
- D<sub>max</sub>, *i.e.*, the maximum size of the drop measured
- D<sub>min</sub>, *i.e.*, the minimum size of the drop measured
- 11. *n*, *a*, constants of Best's formula  $a = AR'^p$  (*A*, *p* constants)
- 12. G(n) = Radar reflectivity coefficient=  $D_n^{-3} \Sigma N_D D^6 / \Sigma N_D D^3$ , a quantity dependant on spectrum breadth, the median volume diameter  $D_n$  (mm)
- 13. Number of drops sampled
- 14.  $\overline{V/V_0}$  = Weighted fall velocity given by Atlas (1957)

$$R' = \cdot 0036 \ V_0 \ (\overline{V}/V_0) \ W \tag{3}$$

 $V_0$  = Fall velocity of medium volume size in Eq. (3).

15. Calculated value of  $D_n = 0.69^{1/n}a$ ; we obtain  $D_n$  as a solution of Best's equation (1)

*i.e.*, 
$$\frac{1}{2} = \exp \left[-(x/a)^n\right]$$
  
 $D_n = a \ (\log 2)^{1/n}$   
 $D_n = D_{50} = 0.69^{1/n} \ a$  (4)

16. Calculated value of 
$$D_p = a \left(\frac{n-1}{n}\right)^{1/n}$$

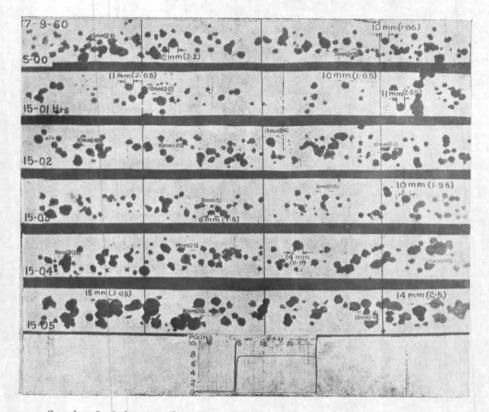
The volume of water comprised by drops with diameter between x and  $x + \Delta x$  is given by

$$W \frac{\partial F}{\partial x} \bigtriangleup x = W \frac{n x^{n-1}}{\bigtriangleup n} \exp \left[ -(x/a)^n \right] \bigtriangleup x$$
(5)

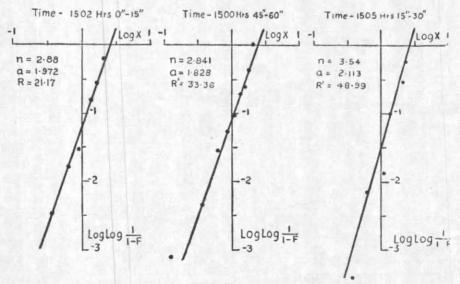
The value of  $D_p$  is that value of x which gives maximum value to the right hand side of Eq. (5), *i.e.*,

$$D_p = a (1-1/n)^{1/n} = a \left(\frac{n-1}{n}\right)^{1/n}$$
 (6)

# RELATION OF RAINDROP SIZE TO INTENSITY OF RAINFALL



Samples of raindrop records at Poona on 17 Sep 1960 during a sharp shower



Poona-Heavy showers without thunder, 17 Sep 1960

F-Fraction of liquid water in the air comprised by drops of diameter less than x (mm) Fraction of volume of water as a function of drop size

Fig. 1

## TABLE

Summary of rain samples taken with the raindrop recorder during shower

S. No.	Date		'ime IST)	<i>R'</i> (mm, <b>hr</b> )	W (mgm/m <sup>8</sup> )	Z (mn. <sup>6</sup> /m. <sup>3</sup> )	D <sub>n</sub> (mm)	$D_n = 0.69^{1/n} \times a$	$D_p$
			* *		,				-
1	17-9-1960	1500	00-15	$27 \cdot 48$	$1307 \cdot 64$	18424 · 3	$2 \cdot 0$	1.77	$2 \cdot 45$
2			15-30	$24 \cdot 13$	$1235 \cdot 31$	$12069 \cdot 6$	1.5	1.38	$1 \cdot 35$
3			30-45	$19 \cdot 05$	$963 \cdot 01$	$11896 \cdot 2$	1.6	$1 \cdot 89$	$2 \cdot 45$
4			45-60	33.36	$1624 \cdot 45$	$18835 \cdot 5$	1.8	1.61	$2 \cdot 15$
5		1501	00-15	$13 \cdot 49$	$688 \cdot 78$	$6057 \cdot 1$	1.5	1.44	1.85
6			15-30	9.06	587.73	$4037 \cdot 1$	1.3	1.19	$1 \cdot 50$
7			30-45	$7 \cdot 13$	$384 \cdot 01$	$2598 \cdot 3$	$1 \cdot 5$	1.73	1.20
8			45-60	$13 \cdot 97$	$684 \cdot 40$	6629 - 7	1.7	$1 \cdot 62$	1.85
9		1502	00-15	$21 \cdot 17$	$1022 \cdot 10$	$10629 \cdot 7$	1.7	1.73	1.85
10			15-30	20.78	1094.86	8154.4	1.3	1.69	1.41
11			30-45	$21 \cdot 45$	1140.40	9879.5	1.3	1.52	1.37
12			45-60	$28 \cdot 41$	$1312 \cdot 05$	$16453 \cdot 3$	1.3	$2 \cdot 02$	$2 \cdot 11$
13		1503	00-15	$20 \cdot 95$	$994 \cdot 92$	$13367 \cdot 3$	1.5	$1 \cdot 57$	1.10
14			15-30	$14 \cdot 30$	$781 \cdot 54$	$4482 \cdot 9$	1.3	$1 \cdot 61$	1.39
15			30-45	10.98	622+63	$3935 \cdot 4$	1.3	1.53	1.35
16			45-60	$15 \cdot 02$	$798 \cdot 41$	$5074 \cdot 4$	$1 \cdot 3$	$1 \cdot 83$	1.70
17		1504	00-15	24.98	$1231 \cdot 15$	$13166 \cdot 5$	1.5	1.78	$1 \cdot 85$
18			15-30	$28 \cdot 10$	$1335 \cdot 32$	$17500 \cdot 6$	$1 \cdot 5$	1.68	1.70
19			30-45	$23 \cdot 21$	$1081 \cdot 90$	$14831 \cdot 6$	$1 \cdot 7$	$2 \cdot 02$	1.43
20			45-60	$16 \cdot 91$	$803 \cdot 38$	8932.0	1.7	1.76	1.85
21		1505	00-15	39.73	1649.79	$41097 \cdot 4$	$2 \cdot 0$	2.11	$2 \cdot 02$
21 20		1000	15.30	$48 \cdot 99$	$2032 \cdot 94$	$48549 \cdot 9$	2.3	$1 \cdot 90$	2+40
20			30-45	$27 \cdot 42$	$1260 \cdot 46$	$17955 \cdot 9$	2.0	1.75	2.10

Date	Type of rain		Sample taken with dyed Whatman No. 1 filter paper tape
17-9-60	Sample of shower type of rain (cumuliform clouds)	R'	: Rate of rainfall (mm/hr)
11 0 00		W	: Liquid water content (mgm/m <sup>3</sup> )
19-9-60	Sample of continuous type of rain (stratiform and	Z	: Radar reflectivity (mm <sup>6</sup> /m <sup>3</sup> )
10 0 00	cumuliform clouds mixed)	G(n)	: Reflectivity coefficient
26-6-60	Sample of non-freezing rain (stratiform clouds)	$\overline{V}/V_0$	: Weighted fall velocity given by equa

 $\overline{V}/V_0$ : Weighted fall velocity given by equation (8)

type of rain (cumuliform clouds) without thunder at Poona

$=a\left[\frac{(n-1)}{n}\right]$	$ ^{1/n} D_m$	D <sub>d</sub>	$D_v$	$D_{\max}$	D <sub>min</sub>	n	a	Reflectivity coefficient G(n)	Drops sampled	- <u></u> <i>V</i> / <i>V</i> ,
$2 \cdot 02$	1.17	0.65	1.44	2.5	0.35	$2 \cdot 34$	2.07	0.922	35	0.8995
1.37	0.91	0.57	$1 \cdot 23$	2.5	0.20	2.50	1.67	1.516	47	$1 \cdot 0029$
1.99	0.91	0.63	$1 \cdot 23$	2.4	0.35	$2 \cdot 33$	$2 \cdot 04$	$1 \cdot 521$	38	0.9725
1.80	1.03	0.62	$1 \cdot 34$	2.4	$0 \cdot 20$	$2 \cdot 84$	1.83	$1 \cdot 095$	51	0.9507
1.28	1.03	0.63	1.27	2.1	0.35	3.72	1.59	1.365	23	1.0056
1.33	0.85	0.62	$1 \cdot 10$	2.2	0.35	3.00	1.35	$1 \cdot 842$	30	0.9111
1.35	0.79	0.70	1.08	1.9	0.20	1.79	2.13	1.050	20	0.9533
1.82	1.13	$1 \cdot 30$	$1 \cdot 33$	$2 \cdot 1$	0.35	2.75	1.85	0.947	19	0.9450
1.94	1.24	1.85	1.44	2.2	0.35	2.88	1.97	1.016	25	0.9589
1.90	1.11	1.41	$1 \cdot 28$	1.9	0.35	2.88	1.93	1.997	36	1.1217
1.53	1.07	0.63	$1 \cdot 25$	2.4	0.35	$3 \cdot 51$	1.69	2.323	39	1.1117
2.32	1.39	$2 \cdot 11$	$1 \cdot 57$	$2 \cdot 2$	$0 \cdot 20$	2.38	2.37	3.362	25	0.9662
1.52	1.26	1.11	1.44	2.7	0.55	2.81	1.79	2.085	24	1.0812
1.77	$1 \cdot 50$	1.38	1.27	1.9	0.55	2.67	1.85	1.538	26	1.1246
1.74	0.92	0.66	1.09	1.3	0.35	$2 \cdot 54$	1.77	1.695	28	1.0423
2.08	1.14	1.33	1.29	1.9	0 • 20	$2 \cdot 42$	2.13	1.704	25	1.1119
2.03	1.05	0.58	1.31	2.1	0.20	$2 \cdot 50$	2.07	1.659	39	1.0418
1.87	$1 \cdot 32$	$1 \cdot 70$	1.53	2.7	0.35	3.00	$1 \cdot 91$	$2 \cdot 033$	29	1.0805
2.09	1.37	1.43	1.56	2.2	0.35	$3 \cdot 45$	$2 \cdot 25$	1.339	23	0.9932
1.96	$1 \cdot 25$	1.40	1.48	2.2	0.35	3.00	1.99	1.086	19	0.9745
2.12	1.53	1.38	1.80	3.1	0.35	3.22	2.37	1.630	23	1.0307
$1 \cdot 92$	1.50	1.48	1.89	2.8	0.35	$3 \cdot 54$	$2 \cdot 11$	$1 \cdot 097$	26	0.9701
1.77	1.32	0.68	1.16	2.5	0.55	3.48	1.95	0.932	27	0.9311

Sample taken with dyed Whatman No. I filter paper tape

 $D_n$ : Median volume diameter

- $D_m$ : Mean diameter
- $D_d$ : Mode diameter

 $D_v$  : Mean volume diameter

Dp : Predominant diameter

n, a : Constants of Best's tormulaa :  $AR'^p$  (A, p constants) $D_{\max}$  : Maximum diameter $D_{\min}$  : Minimum diameter

## TABLE

Summary of rain samples taken with the raindrop recorder during continuous type of rain

s.	Date		Time	R'	W	Z	$D_n$	$D_n =$	$D_p$
No.			(IST)	(mm/hr)	$(mgm/m^3)$	$(mm^{6}/m^{3})$	(mm)	$0 \cdot 69 \ ^{1/n} \times a$	
1	19-9-1960	1650	00-15	16.40	816.97	8142.8	$1 \cdot 5$	$1 \cdot 50$	$1 \cdot 27$
2			15-30	$7 \cdot 03$	$386 \cdot 44$	$2299 \cdot 0$	$1 \cdot 3$	$1 \cdot 30$	$1 \cdot 28$
3		1651	00-15	7.10	$492 \cdot 73$	$2571 \cdot 2$	$1 \cdot 1$	0.98	0.64
4			15-30	14.31	$586 \cdot 01$	$21110 \cdot 1$	$1 \cdot 9$	1.66	3.24
5			45-60	$50 \cdot 04$	$1833 \cdot 48$	$122097\cdot 2$	$2 \cdot 6$	2.72	3 · 92
6		1656	00-15	$18 \cdot 43$	$825 \cdot 21$	15771.5	$1 \cdot 7$	$1 \cdot 89$	2.63
7			15-30	$28 \cdot 32$	$1084 \cdot 21$	$44954 \cdot 1$	$2 \cdot 4$	$2 \cdot 52$	3.30
8			30-45	18.51	831.56	$22307 \cdot 5$	$1 \cdot 9$	1.60	1.56
9			45-60	$67 \cdot 00$	$2369\cdot 12$	$211939 \cdot 4$	$2 \cdot 9$	$2 \cdot 79$	4.03
10		1657	00-15	34.00	1310.81	70479 • 1	$2 \cdot 3$	$2 \cdot 19$	$2 \cdot 40$
11			30-45	$14 \cdot 91$	$751 \cdot 25$	$13344 \cdot 7$	$1 \cdot 6$	1.17	1.23
12			45-60	$40 \cdot 42$	$1764\cdot 83$	$55002 \cdot 7$	$1 \cdot 9$	$1 \cdot 56$	1.36
13		1658	00-15	13.13	702 • 19	8657.3	1.4	1.59	0 • 62
14			15-30	$11 \cdot 50$	634 • 18	5087.8	$1 \cdot 6$	1.25	1.86
15			30-45	$7 \cdot 63$	$410 \cdot 29$	3855 . 6	$1 \cdot 5$	1.33	$2 \cdot 02$
16			45-60	$10 \cdot 52$	$568 \cdot 54$	5772·1	$1 \cdot 6$	$1 \cdot 32$	0.98
17		1659	00-15	21.50	978.13	17091.5	1.9	1.71	1.60
18			15-30	10.08	$539 \cdot 85$	5373.8	$1 \cdot 5$	1.32	1.14
19			30-45	7.01	400.88	3041.1	$1 \cdot 5$	1.26	1.56

#### TABLE

Summary of rain samples taken with the raindrop recorder

1	26-6-1960	1043	00-15	$4 \cdot 59$	315.01	909.3	1.0	1.04	1-10
2			15 - 30	7.64	399.71	$4475 \cdot 4$	1.1	$1 \cdot 22$	0.8
3			30-45	7.74	$493 \cdot 28$	1526.6	$1 \cdot 0$	1.26	1.4
4			45-60	$13 \cdot 77$	718.61	$6017 \cdot 5$	$1 \cdot 5$	1.59	1.8
5		1044	00-15	11.11	640.48	3901.9	1.3	1.30	1.4
6			15-30	15.77	798.27	7174.8	1.5	1.84	1.8
7			45-60	$4 \cdot 94$	$372 \cdot 01$	$738 \cdot 6$	0.7	0.93	0.8
8		1045	00-15	$2 \cdot 52$	199.14	390.9	0.7	1.06	0.5
9			15-30	8.47	438.37	4888.3	1.9	1.83	2.1
10			30-45	$2 \cdot 42$	149.17	627.8	$1 \cdot 0$	1.15	0.8
11			45-60	9.07	$446 \cdot 70$	7095.3	1.3	1.27	0.9

<sup>2</sup> 

$D_p =$	$a\left[\frac{n-1}{n}\right]^{1/n}$	Dm	D <sub>d</sub>	D <sub>v</sub>	D <sub>max</sub>	D <sub>min</sub>	n	a	Reflectivity coefficient G(n)	Drops sampled	$\overline{V}/V_{0}$
	1.55	1.21	0.09	1.37	2.40	1.21	4.00	1.67	1.55	20	1.03
	1.32	1.18	1.13	1.28	1.85	0.64	2.74	1.44	1.59	12	1.08
	0.89	0.74	0.64	0.89	2.18	0.50	3.20	1.00	1.92	40	1.12
	1.66	1.14	0.68	$1 \cdot 59$	$3 \cdot 24$	0.20	3.32	1.85	2.86	13	1.08
	2.60	1.29	0.62	1.94	3.92	0.48	2.52	3.16	1•98	25	1.00
	1.87	1.19	1.12	1.51	2.71	0.32	3.00	2.14	1.87	19	1.05
*	2.43	1.48	0.87	1.97	3.30	0.37	2.68	$2 \cdot 89$	$1 \cdot 62$	13	1.01
	1.55	1.09	0.63	1.44	3.02	0.61	2.38	1.86	2.13	22	0.98
	2.64	1.28	1.20	2.02	4.08	0.24	2.54	3.24	1.97	28	0.98
	2.20	1.33	0.62	0.71	3.00	0.48	3.30	2.45	1.75	18	1.03
	1.18	0.89	0.62	1.18	2.81	0.27	3.34	1.31	2.17	32	0.98
	1.27	1.06	0.66	1.45	3.69	0.20	1.90	1.99	2.48	52	1.01
	1.53	0.83	0.62	1.12	2.67	0.20	2.70	1.82	2.48	35	1.01
	1.18	0.94	1.16	1.16	$2 \cdot 17$	0.37	$2 \cdot 50$	1:45	$1 \cdot 62$	29	1.00
	1.13	0.65	0.40	0.96	$2 \cdot 02$	0.09	2.00	1.60	1.46	29	0.95
	1.25	0.87	0.66	1.13	2.48	0.31	2.56	$1 \cdot 52$	1.24	29	0.90
	1.25	1.16	0.82	1.45	2.66	0.43	3.12	1.93	1.39	24	0.97
	0.71	0.91	1.14	1.12	2.41	0.33	2.82	$1 \cdot 50$	1.55	23	0.96
	1.13	0.83	0.46	1.04	2.06	0.28	2.34	1.48	1.18	22	0+90

with thunder (cumuliform and stratiform clouds mixed) at Poona

3

during continuous non-freezing rain at Poona

1012				1000						
1.05	0.87	0.85	0.95	1.70	0.63	3.00	1.07	1.51	19	1.(
1.23	1.00	0.81	1.20	$2 \cdot 33$	0.60	<b>4</b> .00	1.33	4.12	15	1.5
1.17	0.92	0.84	1.02	$1 \cdot 50$	0.50	3.60	1.28	1.62	27	1.
1.58	1.06	0.65	1.24	1.84	0.56	2.70	1.61	1.30	24	0.9
1.21	1.01	0.83	1.14	2.18	0.53	3.64	1.32	1.63	27	0.9
1.86	1.17	0.91	1.34	2.20	0.51	3.75	2.02	1.39	23	1.
0.95	0.77	0.67	0.83	1.30	0.39	4.00	1.02	2.46	30	1.2
1.06	0.66	0.57	0.79	1.50	0.38	3.00	1.08	2.44	19	1.
1.82	0.86	0.65	1.17	$2 \cdot 20$	0.13	2.75	1.78	0.89	20	0.8
1.15	0.97	0.81	1.07	2.70	0.65	3.16	1.17	2.20	7	1.(
1.30	1.12	0.91	1.36	2.65	0.73	5.20	1.36	2.17	14	1.1

TA	<b>D</b> 1	122		
1 A	151	184	4	
			_	

\*Median volume diameter Dn, liquid water content W, radar echo intensity Z, as a function of rain intensity computed from various sources with additional tropical data from India

Source	D <sub>n</sub> (mm)	W (mgm/m <sup>3</sup> )	$Z = \sum_{ND} D^{68D}$ $= CR^{'n}$
Jones (1956), Illinois (Heavy rain showers)	1.48 R' 0.05	52 R' 0.97	3588.1 :6
Boucher (1951), Cambridge, Mass. (Showers, thunderstorms, widespread rain both uniform and variable)	-	9-12	180R' 1.55
Higgs (1952), Australia (Showers)	-	-	127R' 2. 37
Srivastava and Kapoor (1961), New Delhi			
(a) Widespread rain with melting band	1.22R' 0.16	_	277 R' 1.54
(b) Rain showers from tall convective clouds not showing melting band	-	-	197 <i>R'</i> <sup>1-70</sup>
Kelkar (1961), Poona (General rains)	Average size		
	$Dn = 0.80 R'^{0.27}$ $Dm = 0.63 R'^{0.25}$	71 R' 0.88	189 R' 1.25
	$De = 0 \cdot 79R^{\prime 0 \cdot 21}$		
	Jones (1956), Illinois (Heavy rain showers) Boucher (1951), Cambridge, Mass. (Showers, thunderstorms, widespread rain both uniform and variable) Higgs (1952), Australia (Showers) Srivastava and Kapoor (1961), New Delhi (a) Widespread rain with melting band (b) Rain showers from tall convective clouds not showing melting band	$D_n$ (mm)Jones (1956), Illinois (Heavy rain showers) $1 \cdot 48 \ R'^{0.05}$ Boucher (1951), Cambridge, Mass. (Showers, thunderstorms, widespread rain both uniform and variable) $-$ Higgs (1952), Australia (Showers) $-$ Srivastava and Kapoor (1961), New Delhi (a) Widespread rain with melting band $1 \cdot 22R'^{0.16}$ (b) Rain showers from tall convective clouds not showing melting band $-$ Kelkar (1961), Poona (General rains) $A * erag : size$ $Dn = 0 \cdot 80R'^{0.27}$	$D_{n}$ $W$ (mm) $W$ (mgm/m <sup>3</sup> )Jones (1956), Illinois (Heavy rain showers) $1 \cdot 48 \ R' \ 0 \cdot 05$ $52 \ R' \ 0 \cdot 97$ Boucher (1951), Cambridge, Mass. (Showers, thunderstorms, widespread rain both uniform and variable) $ -$ Higgs (1952), Australia (Showers) $ -$ Srivastava and Kapoor (1961), New Delhi (a) Widespread rain with melting band $1 \cdot 22R' \ 0 \cdot 16$ $-$ (b) Rain showers from tall convective clouds not showing melting band $ -$ Kelkar (1961), Poona (General rains) $Averag : size$ $D_m = 0 \cdot 80R'^{0 \cdot 27}$ $D_m = 0 \cdot 63R'^{0 \cdot 25}$ $71 \ R' \ 0 \cdot 88$

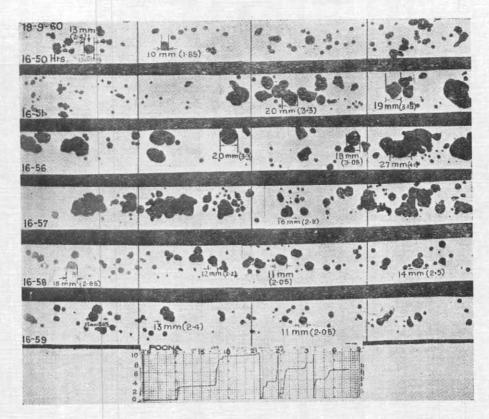
\*Sivaramakrishnan's earlier paper (1961) may also be seen in this connection

#### TABLE 5

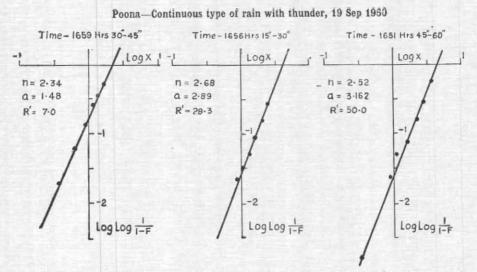
# Regression equations and rainfall parameter for different types of rain at Poona (Sivaramakrishan and Miss Selvam)

Date	Type of rain	Average size $-R'$	WR'	Z-R'	V/V <sub>o</sub>	G(n) (mean)	n (mean)
17-9-60	Shower type without thunder (cumuliform clouds)	$\begin{array}{l} D_n = 0 \cdot 8^{\gamma} R'^{0} \cdot ^{23} \\ D_d = 0 \cdot 45 R'^{0} \cdot ^{24} \\ D_m = 0 \cdot 52 R'^{0} \cdot ^{26} \\ D_y = 0 \cdot 65 R'^{0} \cdot ^{24} \\ D_p = 0 \cdot 76 R'^{0} \cdot ^{27} \end{array}$	W=88.3R' 0.81	$109R'^{1.52}$	$1 \cdot 01$	1.55	2.85
19-9-60	Continuous type with thunder (stratiform and cumuliform clouds mixed)	$\begin{array}{l} D_n = 0.71 R'^{0.32} \\ D_d = 0.57 R'^{0.1} \\ D_m = 0.54 R'^{0.23} \\ D_{\vartheta} = 0.56 R'^{0.31} \\ D_{\varrho} = 0.41 R'^{0.55} \end{array}$	W=81·1R' 0.81	65 <i>R'</i> 1.91	1.00	1.83	$2 \cdot 79$
26-6-60	Non-freezing rain (stratiform elouds)	$\begin{array}{l} D_n = 0 \cdot 59 R'  {}^{0} \cdot {}^{33} \\ D_d = 0 \cdot 65 R'  {}^{0} \cdot {}^{09} \\ D_m = 0 \cdot 65 R'  {}^{0} \cdot {}^{19} \\ D_v = 0 \cdot 71 R'  {}^{0} \cdot {}^{23} \\ D_p = 0 \cdot 42 R'  {}^{0} \cdot {}^{52} \end{array}$	W=87·3 R' 0.80	104.2 <i>R'</i> 1.60	1.06	1.97	3•5

# RELATION OF RAINDROP SIZE TO INTENSITY OF RAINFALL



Samples of raindrop records taken at Poona on 19 Sep 1960 during a severe thunderstorm



F--Fraction of liquid water in the air comprised by drops of diameter less than x (mm) Fraction of volume of water as a function of drop size

Fig. 2

Table 4 gives a summary of the regression equation and rainfall parameters for different types of rain as a function of rain intensity computed from various sources for comparison with the data obtained at Poona.

## 4. Ayalysis of results

# Relation of intensity of rainfall R' with distribution of raindrops $N_D$ for different types of rain at Poona

Fig. 3 shows the raindrop distribution a during a convective shower type of rain on 17 September 1960 without thunder (cumuliform clouds at the time of shower). As can be seen from the weather diary the rain has occurred from cumuliform clouds and that —

(1) For very low intensity, viz., 7 mm per hour the curve is more or less a straight line without peaks and troughs and in general agreement with that given by the empirical relationship of Marshall and Palmer (1948).

(2) As the rainfall rate increases, the curve instead of being a straight line consists of a number of peaks and troughs as noticed by previous investigators (Mason 1953, Blanchard 1953, Ramana Murthy and Gupta 1959, Mason and Andrews 1960, Sivaramakrishnan 1961). One explanation for the peaks and troughs observed during thunderstorm rain at Poona given by Sivaramakrishnan (1961) is due to a marked discontinuity in the updraft rate with the maximum occurring at a certain level which acting as a sort of barrier to falling raindrops below a certain size will cause maximum concentration of raindrops belonging to a particular size group. Two other explanations are also possible for the peaks and troughs noticed. The first is due to wind shear in the atmosphere. With wind shear, and the fact that the drops that are collected at a given spot and time on the ground may have various positions of origin within the cloud, one might conceive of ways in which the drop distribution can vary with drop size. The other explanation may be in the fact that the drop distribution may not contain enough drops in a given sample to be representative of the entire population of drops.

(3) Marshall and Palmer have given the following expression connecting drop concentration and drop diameter for stratiform type of rainfall originating as snow —

$$N_D = N_0 \ e^{-\Delta D} = N_0 \ e^{-3 \cdot 67 D/D_n} \tag{7}$$

where D is drop diameter,  $N_D \delta_D$  is the number of drops of diameter between D and  $D + \delta D$  per unit volume of space and  $N_0$  is the value of  $N_D$ for D = 0,  $N_0 = 0.08$  cm<sup>-4</sup> for any intensity of rainfall and  $\triangle = 3 \cdot 67/D_n = 41 \ R'^{-0.21} \ \mathrm{cm}^{-2}$ where R' is the rainfall rate in mm/hr and  $D_n$  is the median value diameter. The relation of  $\triangle$  to  $D_n$  is due to Altas (1953).

Mueller and Jones (1960) show that Eq. (8) is not applicable to convective showers in Florida. They show that instead of decreasing exponentially with size throughout, the number of drops increases exponentially to a maximum and then drops exponentially from there. The intersection point of the two exponentials occurs close to D =1.5 mm. Rainfall rate in these storms is a more sensitive function of the total number of drops than of the slope. Atlas (1963) has fitted a simple linear relation to the  $(N_t - R')$  curve presented by Mueller and Jones with the result  $N_t = 100 + 7k'$ , where  $N_t$  is the total number of drops per m<sup>3</sup> and R' is the rainfall rate in mm/hr. This compares to  $N_t = 1.95 \times 10^3 R'^{0.21}$  for the Marshall and Palmer (M.P.) distribution.

(4) A similar characteristics of peaks and troughs is also found in the drop spectra in the other two types of rain discussed (Fig. 3).

Relation of intensity of rainfall R' with liquid water content W in different types of rain

By the method of least squares the following relations between W and R' have been obtained for the different types of rain—

1.  $W = 88 \cdot 3R'^{0.81}$ 

for shower type of rain from cumuliform clouds

2.  $W = 81 \cdot 1R'^{0.81}$ 

for continuous type of rain with occasional thunder from stratiform and cumuliform clouds (mixed)

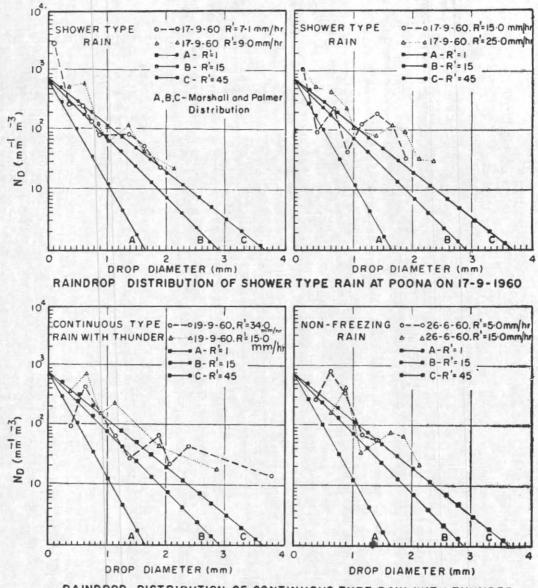
3. W=87.3R'0.80

for non-freezig rain from stratiform clouds.

Relation of intensity of rainfall R' with average size diameter  $(D_d, D_m, D_v, D_n, D_p)$  in different types of rain

By the method of least squares the following relationship between the average size of raindrop and R' has been obtained for the different types of rain. The average size of raindrop can be represented by—

 $D_d$  (mode diameter),  $D_m$  (mean diameter),  $D_v$ (mean volume diameter),  $D_n$  (median diameter),  $D_p$  (predominant diameter)



RAINDROP DISTRIBUTION OF CONTINUOUS TYPE RAIN WITH THUNDER (STRATIFORM AND CUMULIFORM CLOUDS) AND NON-FREEZING- RAIN (STRATIFORM CLOUDS) ON 19-9-1960 AND 26-6-1960 RESP. AT POONA

Fig. 3

M.V. SIVARAMAKRISHNAN AND (MISS) M. MARY SELVAM

	Type of rain	
Shower	Continuous	Non-freezing
0.45R'0.24	0.57 R'0.10	0-658'0.09
$0.52 R'^{0.26}$	0.54 R'0.23	$0 \cdot c5 R'^{0 \cdot 19}$
$0.65 R'^{0.24}$	0.56 8'0.31	$0.71 R'^{0.23}$
$0.80 R'^{0.23}$	0.718.0.32	$0.59 K'^{0.33}$
0.768'0.27	$0.41 R'^{0.50}$	$0.42 R'^{0.52}$
	0.45R'0.24 0.52R'0.26 0.65R'0.24 0.80R'0.23	Shower         Continuous           0.45R'0.24         0.57R'0.10           0.52R'0.26         0.54R'0.23           0.65R'0.24         0.56R'0.31           0.80R'0.23         0.71R'0.32

The above values have been plotted in Fig. 4(a). It will be seen that for the same rate of rainfall, mode diameter is lowest for all types of rain in the following order  $D_d$ ,  $D_m$ ,  $D_v$ ,  $D_n$ ,  $D_p$ .

Atlas (1957) has shown that

$$R' = 0036 \times V_0 \left( V/V_0 \right) \times W \tag{8}$$

where,  $V_0 =$ fall valocity of median volume size,  $\overline{V}/V_0$  = weighted fall velocity defined by Eq. (8) itself. He as well as the author (Sivaramakrishnan 1961) have found that for most raindrop spectra  $\overline{V}/V_0$  falls very close to 1. From Tables 1 to 4 the ratio  $\overline{V}/V_0$  is found to be very close to 1 which clearly shows that a drop distribution in general can be better represented by a uniform collection of drops with size equal to the median volume diameter  $D_n$ . Best (1951) has also shown from his study of drop size distribution in clouds that if n is not known,  $D_m$  and  $D_v$  are quite unsuitable for specifying the mean drop size not only because they vary with the minimum measurable diameter but also, they vary considerably with In this respect he has concluded that  $D_n$  is n. better than any other representation of average size.

## Radar reflectivity factor and intensity of rainfall

The power received at a radar from a rain target is proportional to the radar reflectivity factor  $Z = \Sigma N_D D^6 \delta D$ , where N is the number of drops per cubic metre of diameter D on the size interval  $\delta D$ .

Values of  $Z = \Sigma N_D D^6 \delta D$  have been tabulated in Tables 1 to 3 for different types of rain and plotted in Fig. 4(b). By the method of least squares, the following relations between radar reflectivity factor Z and R' have been determined for the different types of rain and plotted in Fig. 4(b).

$Z = \Sigma N_D D^6  \delta D = C R'^n$
$109 \cdot 0 R'^{1 \cdot 52}$
$65 \cdot 6 R'^{1 \cdot 91}$
$104 \cdot 2 \ R'^{1 \cdot 60}$

Bartnoff and Atlas (1951) have given a basic equation for Z (The radar Reflectivity Factor) as follows—

$$Z = \frac{6}{\pi} G(n) \cdot D_n^3 \quad \frac{W}{\rho} \text{ mm}^6/\text{m}^3$$
 (9)

where,  $D_n =$  Median volume diameter in mm W = Liquid water content in mgm/m<sup>3</sup>  $\rho =$  particle density in gm/cc

 $G(n) = \text{Reflectivity coefficient} = D_n - 3 \Sigma N_D D^6 / \Sigma N_D D^3$ , a quantity dependant on spectrum breadth. G is typically found between 1.5 and 3.0 for the different types of rain.

The mean values of G(n) for the different types of rain discussed here are given below—

Type of rain	Mean value of $G_n$
Shower type	1.55
Continuous type	$1 \cdot 83$
Non-freezing type	$1 \cdot 97$
Relation between Z and W	
Type of rain	$Z = a \; W^b$
Shower type	$0.73 \times W^{1.89}$ (a)
Continuous type	$0.55 \times W^{2.48}$ (b)
Non-freezing type	$0.69 \times W^{2.00}$ (c)

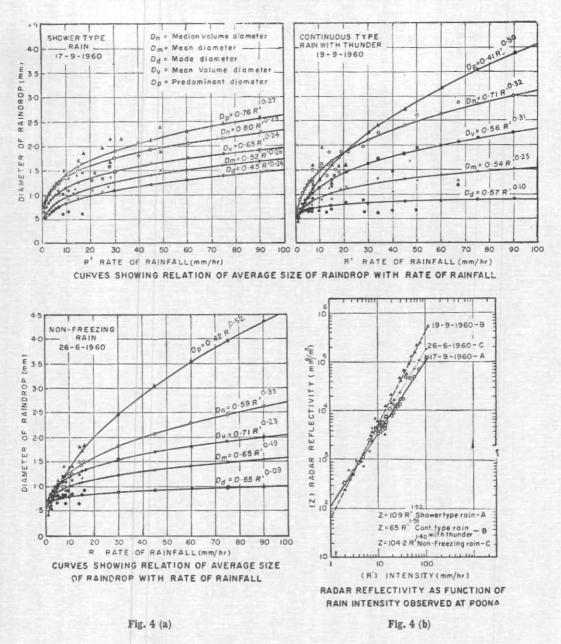
Equations (a), (b), (c) are useful in estimating liquid water content (LWC) from radar measurements of Z provided there are negligible updrafts to alter the size distribution from that observed at the ground. This assumption is generally valid in stratiform type of rain. It is seen from the above equations that Z is almost directly proportional to  $W^2$  for Poona rains also (cf. Battan 1959).

#### 5. Conclusions

1. From the study of the size distribution of raindrops it is shown that the relation of intensity of rainfall with (1) number of drops per cubic metre  $N_D$ , (2) average size of raindrops ( $D_d$ ,  $D_m$ ,  $D_v$ ,  $D_n$ ,  $D_p$ ), (3) liquid water content W and (4) radar reflectivity is found to be different for the different types of rain taken for study. But it is seen that the regression equation connecting W and R' for the different types of rain studied are not very much different. As regards the relation between Z and R' the regression equation between shower type of rain (without thunder) and non-freezing rain is not very much different.

2. The average size of raindrop is better represented by the median size diameter  $D_n$  than by the other raindrop size parameters  $(D_d, D_m, D_v, D_p)$ . It is interesting to see that the regression equation connecting median size diameter and intensity of rainfall (*i.e.*,  $D_n = 0.80R'^{0.23}$ ) is

### RELATION OF RAINDROP SIZE TO INTENSITY OF RAINFALL



found to be practically same as for thunderstorm rain observed earlier by Sivaramakrishnan (1961) at Poona (viz.,  $D_n = 0.82R'^{0.29}$ ), also Marshall and Palmer distribution (1948) (mostly stratiform type is as reported by Best) gives an expression for  $D_n$  as  $D_n = 0.82 R'^{0.24}$ . Thus while individual samples deviate sharply from the M. P. distribution, it appears that the latter is a fairly good average representation even in the tropics. This has been supported by Atlas also (1963).

3. Best's formula, viz.,  $1-F = \exp\left[-(x/a)^n\right]$ 

is found to be suitable for representing the size distribution of raindrops in the tropics also but with suitable changes in the constants.

## 6. Acknowledgements

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REFERENCES

Atlas, D.	1963	Met. Monogr., 5, 27, pp. 183-186.
	1953	J. Met., 10, pp. 486-488.
Atlas, D. and Chmela, A. C.	1957	Proc. Sixth Weath. Radar Conf., 21-29.
Bartnoff, S. and Atlas, D.	1951	J. Met., 8, pp. 130-131.
Battan, L. J.	1959	Radar Meteorology, Univ. Chicago Press, p. 54.
Blanchard, D. C.	1953	J. Met., 10, pp. 457-473.
Best, A. C.	1950	Quart. J.R. met. Soc., 76, pp. 16-36.
	1951	Ibid., 77, pp. 418-426.
Boucher	1951	Proc. Conf. on Water Resources. Illinois State Water Survey Bulletin, 41, pp. 293-297.
Fujiwara, M.	1960	Proc. Eighth Weath. Radar Conf., pp. 159-166.
Gunn, K. L. S. and Marshall, J. S.	1955	J. Met., 12, pp. 339-349.
Higgs	1952	Proc. Third Radar Weather Conf. (Montreal Mc Gill University), pp. D49-D50.
Imai, I.	1956	Pap. in Met. and Geophys., Met. Res. Inst., Japan, pp. 107-123.
Imai, 1., Fujiwara, M. and Toyama, Y.	1955	Pap. in Met. and Geophys., Met. Res. Inst., Japan, 6, pp. 130-139.
Jones, D. M. A.	1956	Res. Rep., 6, Illinois State Water Survey, April 1956, 20 pp.
Kelkar, V. N.	1961	Indian J. Met. Geophys., 12, pp. 553-559.
Laws, J. O. and Parsons, D. A.	1945	Trans. Amer. geophys. Un., 42, pp. 452-460.
Marshall, J. S. and Palmer, W. Mck.	1948	J. Met., 5, pp. 155-166.
Mason, B. J. and Ramanadhan, R.	1953	Quart. J.R. met. Soc., 79, pp. 490-495.
Mason, B. J. and Andrews, J. B.	1960	Ibid., 86, pp. 346-353.
Mueller, E. A. and Jones, D. M. A.	1960	Proc. Eighth Weath. Radar Conf., pp. 299-305.
Ramana Murthy, Bh. V. and Gupta, S. C.	1959	J. Sci. industr. Res., 18A, pp. 353-371.
Rigby, E. C., Marshall, J. S. and Hitschfeld, W.	1954	J. Met., 11, pp. 362-372.
Sivaramakrishnan, M. V.	1961	Indian J. Met. Goephys., 12, pp. 189-217.
Sivaramakrishnan, M. V. and Sivaraman, K., R.	1962	Ibid., 13, Spl. No. pp. 17-20.
Spilhaus, A. F.	1948	J. Met., 5, pp. 161-164.
Srivastava, R. C.	1960	Indian J. Met. Geophys., 11, pp. 145-152.
Srivastava, R. C. and Kapur, R. K.	1961	Ibid., 12, pp. 93-102.