Rainfall distribution in India in relation to latitude, longitude and elevation

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ABSTRACT. An analysis of the normal rainfall of 167 observatory stations distributed over India and the neighbourhood has been made using regression equations representing monthly and annual rainfall as a linear function of latitude, longitude and elevation above sea level. The multiple CCs are high, being 0.8 to 0.9 except in some months.

The anomalies after eliminating the systematic variations have also been studied. These bring to light other factors which influence rainfall, viz., the orographic effects and the effect of lee-side of mountains.

1. Introduction

Jagannathan (1948a, 1948b) studied the distribution of the mean temperature and the mean diurnal range of temperature in India by expressing them as linear functions of latitude, longitude and height above mean sea level of the stations with the data of 167 meteorological stations distributed over India and neighbourhood. He pointed out that similar parameters in respect of any element associated with the same set of stations could easily be obtained by utilising the matrix of multipliers he had presented. Derivation of similar parameters in respect of the distribution of rainfall has been attempted here. Rainfall normals in respect of all except three stations mentioned in Table 1 are available in *India met. Dep. Mem.* (1949).

As the alternative stations selected are very close, the same matrix of multipliers has been used for the present purpose. The stations selected and the regions in which they fall are shown in Fig. 1.

2. Method of analysis

The rainfall r of a place has been represented as linear function of latitude L, longitude l and height above mean sea level of the station H for all the twelve months and the year as a whole.

$$r = A + b_1 L + b_2 \, l + b_3 \, H \tag{1}$$

where A, b_1 , b_2 , b_3 are regression coefficients.

The units employed in calculations are latitude 1minute, longitude 1 minute, elevation 1 foot and rainfall 1 cent. The partial regression coefficients of normal rainfall for any month on latitude, longitude and elevation can readily be obtained from the following —

$$bn_1 = m_{11} \Sigma \phi fn + m_{12} \Sigma \lambda fn + m_{13} \Sigma h fn \tag{2}$$

$$bn_2 = m_{21} \Sigma \phi fn + m_{22} \Sigma \lambda fn + m_{23} \Sigma h fn \tag{3}$$

$$bn_3 = m_{31} \Sigma \phi fn + m_{32} \Sigma \lambda fn + m_{33} \Sigma h fn \tag{4}$$

where m_{ij} is the *i*, j^{th} element in the matrix of multipliers and bn_1 , bn_2 , bn_3 are the partial regression coefficients. *n* representing the particular month or the year. ϕ , λ , h are the deviations from

the respective means of latitude, longitude and elevation of the stations, fn the deviation of the mean rainfall of the station from the mean rainfall of the region during the particular month or year considered.

The standard errors of the regression coefficients are $s\sqrt{m_{11}}$, $s\sqrt{m_{22}}$, $s\sqrt{m_{33}}$, where $s^2 = \text{residual variance} = \Sigma (f-f')^2/(n-4)$, where f and f' are observed and calculated deviations for the mean values of rainfall.

The multiple correlation coefficients have been calculated from —

$$R^2 = (b_1 \Sigma \phi f + b_2 \Sigma \lambda f + b_2 \Sigma h f) / \Sigma f^2$$

The regression coefficients and the standard errors for the different months and the year have been tabulated along with the multiple correlation coefficients (Tables 2-5). In this study generally 5 per cent level of significance has been used for testing.

3. Discussion

Region I — This region consists of the western half of the Peninsula in the tropics. The regression on latitude is significant in all months except in August and September. The negative values indicate that the rainfall decreases as we go northwards. The regression in longitude is insignificant. The elevation regressions are not significant except in January when it is significantly positive and in June when it is significantly negative.

It is significant to note in this connection that the rainfall for January which occurs mostly in the extreme south of the region is due to the passage westwards of storms and depression which form in the Bay of Bengal or due to strong northeast monsoon. The high level stations on the Western Ghats get more rain, and lower level stations get comparatively less rainfall, while in the month of June the majority of the number of high level stations considered are to the lee side of the Ghats which receive less rainfall and thus a negative



Fig. 1. 167 meteorological stations and the four divisions

relationship is indicated.* In July, August and September the multiple correlation coefficients are less than 0.4 and not significant. In June and October they are 0.5 while in the rest of the months they vary from 0.6 to 0.9. The independence of the rainfall with respect to these parameters during the height of monsoon is of interest.

Region $II \rightarrow$ The region comprises of the eastern half of the Peninsula. The southwest monsoon rainfall increases with latitude and northeast monsoon decreases with latitude. The regression on longitude shows a general increase of rainfall towards the coast in these months. The regression on elevation is significantly positive in March and April, and July, August and September. The multiple CCs are 0.8 to 0.9 except in December and January when they are 0.6 - 0.7.

Region III — It comprises of northeast India. The regression on latitude is significant and positive in January, February and August indicating that the northerly stations get more rain while in the rest of the months they are not significant. The regression on longitude is significant and positive in all the months except in October, December and January, suggesting that the more easterly stations get more rainfall.

The elevation of the stations does not appear to have any effect on the rainfall except in January and February when the higher level stations get more rainfall. The multiple CCs are all significant and range from 0.5 in August to 0.9 in October.

228

^{*}For a proper understanding of the relationship of elevation and aspect of orography on rainfall, it is necessary to separate out t e windward and leeward sides. This is being studied separately.

_	Stations for which rainfall data are not available			Stations substituted				
	Stations	Lat.	Long.	Ht. (ft)	Stations	Lat.	Long.	Ht. (ft) (approx.)
1. 2. 3.	Rampur Boalia Patiala Chakrata	$\begin{array}{c} 24 \ 22 \\ 30 \ 20 \\ 30 \ 43 \end{array}$	88 36 76 28 77 54	70 818 6922	1. Lalgola 2. Lehal 3. Ambari	24 12 30 22 30 28	88 17 76 22 77 54	60 800 4000

TABLE 1

TABLE 2
Regression coefficients of rainfall on latitude, longitude and height Region I (42 stations)

	B	Multiple correlation		
	Latitude	Longitude	Height	$\stackrel{ m coefficient}{R}$
January	- ·0724± ·0308	$+ \cdot 0078 \pm \cdot 0602$	$+ \cdot 0130 + \cdot 0045$.63
February	$- \cdot 0448 \pm \cdot 0174$	$+ \cdot 0305 \pm \cdot 0341$	$+ \cdot 0039 + \cdot 0026$	• 61
March	$ \cdot 1138 \pm$ $\cdot 0231$	$+ \cdot 0049 + \cdot 0452$	$+ \cdot 0049 + \cdot 0034$.74
April	$- \cdot 4323 \pm \cdot 0485$	$- \cdot 0681 \pm \cdot 0949$	$+ \cdot 0131 + \cdot 0072$.87
May	$9215 \pm .1171$	$- \cdot 2254 \pm \cdot 2291$	0020+.0173	.89
June	$-2 \cdot 2917 \pm \cdot 6756$	-1.3064 ± 1.3217	$- \cdot 2383 + \cdot 0997$.54
July	$-1.5977 \pm .7637$	-1.7584 ± 1.4940	$- \cdot 1775 + \cdot 1127$	-30
August	$- \cdot 7440 \pm \cdot 4430$	$- \cdot 4540 + \cdot 8667$	0700+ .0654	.90
September	$0199 \pm .1835$	$+ \cdot 5422 + \cdot 3595$	- ·0087+ ·0261	.20
October	$-1.1746 \pm .2036$	$- \cdot 1028 + \cdot 3983$	+ .0285++ .0300	. 59
November	$6913 \pm .0929$	$- \cdot 0274 + \cdot 1816$	+ .0211 + .0130	.97
December	$- \cdot 2247 \pm \cdot 0550$	$0109 \pm .1076$	$+ \cdot 0156 \pm \cdot 0081$.69
Annual	$-8 \cdot 1852 \pm 2 \cdot 0298$	$-3 \cdot 3917 \pm 3 \cdot 9706$	$- \cdot 4340 \pm 0 \cdot 2997$	·59

TABLE 3 Regression coefficients of rainfall on latitude, longitude and height Region II (40 s'ations)

	Regre	Regression coefficients of rainfall on			
	Latitude	Longitude	Height	$\stackrel{\text{coefficient}}{R}$	
January	$2147 \pm .0598$	$+ \cdot 1007 \pm \cdot 0678$	$+ \cdot 0200 + \cdot 0176$:63	
February	$+ .0090 \pm .0289$	$+$ $\cdot 1162 \pm$ $\cdot 0328$	+ .0128 + .0085	.78	
March	$- \cdot 0527 \pm \cdot 0335$	$+ \cdot 2668 \pm \cdot 0380$	$+ \cdot 0217 + \cdot 0085$.80	
April	$ \cdot 3837 \pm$ $\cdot 1023$	$+ \cdot 6789 \pm \cdot 1161$	+ .0737 + .0301	-76	
May	$ \cdot 5650 \pm$ $\cdot 2038$	+1.2516+.2312	$+ .1050 \pm .0598$	- 20	
June	$+ \cdot 5668 \pm \cdot 2610$	+1.3063 + .2950	+ 1209 + 10768	-80	
July	$+1.5904\pm.4130$	$+ \cdot 5317 + \cdot 4685$	$+ \cdot 2683 \pm \cdot 1215$	- 90	
August	$+ \cdot 9626 \pm \cdot 3836$	$+ \cdot 8705 + \cdot 4351$	+ + + + + + + + + + + + + + + + + + + +	-81	
September	$+$ $\cdot 3266 \pm$ $\cdot 1929$	$+ \cdot 6074 + \cdot 2188$	+ .1566+ .0567	.94	
October	$-1.1832 \pm .1968$	$+ \cdot 8484 + \cdot 2231$	- :0175 L :0570	•83	
November	-1.5772 + .3206	$+ \cdot 4565 + \cdot 3637$	- ·0113± ·0019	•84	
December	$- \cdot 8558 + \cdot 2013$	+ .3914 + .9989	- ·0227± ·0943	•81	
Annual	-1.3489 ± 1.9809	$+7.4842\pm2.2467$	$+ \cdot 0354 \pm \cdot 0592$ $+ 1 \cdot 0463 \pm 0 \cdot 5827$	·73 ·66	

G. RAMACHANDRAN

	Regre	Multiple correlation		
	Latitude	Longitude	Height	R
January	$+ \cdot 2564 \pm \cdot 0207$	$- \cdot 0125 \pm \cdot 0200$	$+ \cdot 0071 \pm \cdot 0034$	•72
February	$+$ $\cdot 2379 \pm$ $\cdot 0767$	$\div \cdot 0933 \pm \cdot 0234$	$+$ $\cdot 0145 \pm$ $\cdot 0040$	·72
March	$+$ $\cdot 2639 \pm$ $\cdot 1795$	\pm $\cdot 3315 \pm$ $\cdot 0547$	$+$ $\cdot 0120 \pm$ $\cdot 0094$	- 69
April	$+ \cdot 7071 \pm \cdot 3885$	$+$ $\cdot 9248 \pm$ $\cdot 1184$	$+\cdot0778\pm\cdot0202$	-78
May	\pm $\cdot 7719 \pm$ $\cdot 4709$	$+1.5459 \pm .1435$	$+$ $\cdot 0180 \pm$ $\cdot 0245$	· 80
June	$+$ $\cdot 7917 \pm$ $\cdot 7135$	$-1\cdot 8220\pm\cdot 2174$	$+$ $\cdot 0697 \pm$ $\cdot 0371$.80
July	$+1.5043 \pm .8272$	$+ \cdot 8059 \pm \cdot 2521$	$+$ $\cdot 0777 \pm$ $\cdot 0430$	- 53
August	$+1.3857 \pm .6902$	$+$ \cdot 5723 \pm \cdot 2102	$+$ $\cdot 0571 \pm$ $\cdot 0359$	· 50
September	$+$ $\cdot 7797 \pm$ $\cdot 4794$	\pm $\cdot 8707 \pm$ $\cdot 1481$	$+$ $\cdot 0241 \pm$ $\cdot 0249$	- 68
October	$ \cdot 2195 \pm $ $\cdot 1848$	$+ \cdot 5727 \pm \cdot 5630$	\pm $\cdot 0103 \pm$ $\cdot 0096$	-87
November	$- \cdot 1435 \pm \cdot 0960$	$+$ $\cdot 0937 \pm$ $\cdot 0293$	$+$ $\cdot 0048 \pm$ $\cdot 0050$	• 55
December	$+$ $\cdot 0887 \pm$ $\cdot 1031$	$ \cdot$ 0115 \pm \cdot 0314	$+$ $\cdot 0047 \pm$ $\cdot 0054$	· 69
Annual	$\pm 6 \cdot 4052 \pm 2 \cdot 9417$	$+7.7599\pm0.8965$	$+0.2955 \pm 0.1525$	· 80

TABLE 4 Regression coefficients of rainfall on latitude, longitude and height Region III (45 stations)

TABLE 5 Regression coefficients of rainfall on latitude, longitude and height Region IV (40 stations)

	Regression coefficients of rainfall on			Multiple correlation
	Latitude	Longitude	Height	R
January	$+ \cdot 1666 \pm \cdot 0697$	$+ \cdot 0093 \pm \cdot 0619$	$+ \cdot 1040 \pm \cdot 0046$	•68
February	$+$ $\cdot 1501 \pm$ $\cdot 0649$	$- \cdot 0352 \pm \cdot 0577$	$\pm \cdot 0201 \pm \cdot 0043$	•78
March	$+$ $\cdot 3578 \pm$ $\cdot 0896$	$ \cdot 1241 \pm$ $\cdot 0795$	$+ \cdot 0166 \pm \cdot 0059$	•76
April	$+ \cdot 2500 \pm \cdot 0891$	$0829 \pm .0791$	$+ \cdot 0156 \pm \cdot 0059$	·68
Mav	$+$ $\cdot 1034 \pm$ $\cdot 0542$	$+$ $\cdot 0534 \pm$ $\cdot 0481$	$+ \cdot 0105 \pm \cdot 0036$	•66
June	$- \cdot 4402 \pm \cdot 1226$	$+ .5635 \pm .1088$	$+ \cdot 0192 \pm \cdot 0082$.71
July	$-1.6060 \pm .4109$	$+1.5336 \pm .3648$	$+ \cdot 0580 \pm \cdot 0273$	-67
August	$-1.5065 \pm .4130$	$+1.4947 \pm .3666$	$+ \cdot 0802 \pm \cdot 0274$	· 66
Sentember	$- \cdot 6445 \pm \cdot 1638$	$+$ $\cdot 7976 \pm$ $\cdot 1454$	$+ \cdot 0197 \pm \cdot 0109$	$\cdot 73$
October	$+ .0667 \pm .1318$	$+ .0799 \pm .0283$	$- \cdot 0041 \pm \cdot 0021$	· 53
November	$+ .0052 \pm .0129$	$- \cdot 0045 \pm \cdot 0115$	$+ \cdot 0032 \pm \cdot 0008$	· 61
December	$+ \cdot 0845 \pm \cdot 0339$	$ \cdot 0327 \pm $ $\cdot 0301$	$+ \cdot 0081 \pm \cdot 0022$	•72
Annual	$-2 \cdot 9491 \pm 1 \cdot 3412$	$+4 \cdot 1063 \pm 1 \cdot 1907$	$+0.1941\pm .0891$	· 59

RAINFALL DISTRIBUTION IN INDIA



Fig. 4. Anomalies (calculated — observed) of rainfall in inches

Fig. 5. Anomalies (calculated — observed) of rainfall in inches

231



Region IV — This comprises northwest India. The regression on latitude is positive and significant during December to April and significant but negative during June to September indicating that the rainfall during December to April which is due to western disturbances is more to the north while the monsoon rainfall during June to September decreases northwards.

The positive regression on longitude indicates that the rainfall is higher towards east during June to October. The positive regression on elevation is significant except during September and October. The multiple CCs range from 0.5 in October to 0.8 in February. The multiple correlation coefficient R for the annual rainfall is 0.6.

4. Anomalies

With a view to compare rainfall calculated from the regression equations with the actual, the anomalies (calculated *minus* observed) for the four regions were calculated and plotted on the charts. Five of these charts — January, April, July, October and Annual — are shown in Figs. 2–6. These anomaly charts besides indicating the goodness of fit reveal some interesting features which are detailed below. The negative anomalies suggest that we must search for factors other than latitude, longitude and elevation for causing rainfall while positive anomalies indicate other orographic influences which inhibit rainfall.

During December to March the negative anomalies occur over the extreme south of the Peninsula including the Coromandel coast and also a strip of the country extending from Konkan, Kathiawar coast to Orissa and a third over the northwest part of the country extending from west Uttar Pradesh northwestward. To a large extent it can be said that these represent the rainfall due to depressions, devoid of the influence of latitude, longitude and elevation.

Noteworthy areas of positive anomalies are Himalayan regions including Kashmir.

During the hot weather season, April and May, the actual rainfall is more than the calculated over the southern part of west coast, the interior Tamilnad, over Assam and East Pakistan and over the central and northwestern parts outside the arid tracts. This is a season in which rainfall due to local convective phenomena occur with greater intensity over most of the parts mentioned above and the excessive rain is probably accounted by these. The rest of the country exhibits positive anomalies.

During June to September, west coast of the Peninsula, East Pakistan, the sub-Himalayan West Bengal and the central parts of the country exhibit negative anomalies. The positive anomalies on the leeward side of Western Ghats are noteworthy.

During October and November notable regions of positive anomalies are the interior Peninsula and negative anomalies over the coastal regions to the east and southwest of the Peninsula.

The above analysis shows the broad features of the rainfall pattern associated with the latitude, longitude and elevation in the particular regions concerned. However, for a closer understanding of the relationship of rainfall with the orography in particular, the study will have to be restricted to small regions with varied orography. Attempts into this direction are in progress.

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